

ISSN 2310-6697

otoiser—open transactions on independent scientific-engineering research

# FUNKTECHNIKPLUS # JOURNAL

Théorie—Expérimentation—Métrologie—Logiciel—Applications

ISSUE 2 – SUNDAY 17 NOVEMBER 2013 – YEAR 1

REPRINT

## Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 3: Short One-Port Calibration – Comparison

N.I. Yannopoulou, P.E. Zimourtopoulos



*This small European Journal is  
In the Defense of Honesty in Science and Ethics in Engineering*

**Publisher** – otoiser—open transactions on independent scientific engineering research, [www.otoiser.org](http://www.otoiser.org) – [info@otoiser.org](mailto:info@otoiser.org), Hauptstraße 52, 2831 Scheiblingkirchen, Austria

**Language** – We declare the origins of the Journal by using in the cover page English, German and French, as well as, a Hellenic vignette. However, since we recognize the dominance of US English in the technical literature, we adopted it as the Journal's language, although it is not our native language.

**Focus** – We consider Radio–FUNK, which still creates a vivid impression of the untouchable, and its Technology–TECHNIK, from an Advanced–PLUS point of view, Plus–PLUS Telecommunications Engineering, Electrical Engineering and Computer Science, that is, we dynamically focus at any related scientific-engineering research regarding Théorie, Expérimentation, Métrologie, Logiciel, ou Applications.

**Scope** – We emphasize this scope broadness by extending the title of the Journal with a Doppelkreuz-Zeichen # which we use as a placeholder for substitution of our Editorial Team disciplines: # Telecommunications etc. as above, or # High Voltage, # Software Engineering, # Simulation etc. as below.

**Frequency** – We publish 3 issues per year: on 31st of January, on 31st of May, and on 30th of September, as well as, an extra issue every 3 papers and a volume every 2 years.

**Editions** – We increase the edition number of an issue only when is needed to reform one or more of its papers—thus to increase their version numbers—but we keep unchanged its 1st edition date shown on its front page and we number its pages sequentially from 1. We count the editions of *About* separately.

**Format** – We use a fixed-space font, hyphenation, justification, unfixed word spacing, and the uncommon for Journals A5 (half A4) page size to achieve WYSIWYG printing and clear reading of 2 to 4 side-by-side pages on wide-screen displays

**Printing-on-Demand** – We can email gratis PDFs at 300-4000 dpi in booklet page scaling of either brochure or book type.

**Copyright** – We publish under a Creative Commons Attribution, CC-BY 3.0 Unported or CC-BY 4.0 International, License only.

Please download the latest *About* edition from  
[about.ftpj.otoiser.org](http://about.ftpj.otoiser.org)

**Editorial Team****# Electrical Engineering**

# High Voltage Engineering # Insulating Materials

Professor Michael Danikas, mdanikas@ee.duth.gr  
EECE, Democritus University of Thrace, Greece

# Electrical Machines # Renewable Energies # Electric Vehicles

Assistant Professor Athanasios Karlis, akarlis@ee.duth.gr  
EECE, Democritus University of Thrace, Greece

**# Computer Science**

# Computer Engineering # Software Engineering # Cyber Security

Professor Vasilis Katos, vkatos@bournemouth.ac.uk  
Head of Computer and Informatics Dept, Bournemouth Univ, UK

# Internet Engineering # Learning Management Systems

Lecturer Sotirios Kontogiannis, skontog@gmail.com  
Business Administration Dept, TEI, Western Macedonia, Greece

# Hypercomputation # Fuzzy Computation # Digital Typography

Dr. Apostolos Syropoulos, asyropoulos@yahoo.com  
BSc-Physics, MSc-Computer Science, PhD-Computer Science  
Independent Researcher, Xanthi, Greece

**# Telecommunications Engineering**

# Applied EM Electromagnetics # Applied Mathematics

Dr. Nikolaos Berketis, nberketis@gmail.com  
BSc-Mathematics, MSc-Applied Maths, PhD-Applied Mathematics  
Independent Researcher, Athens, Greece

# Antennas # Metrology # EM Software # Simulation # Virtual Labs

# Applied EM # Education # FLOSS # Amateur Radio # Electronics

Dr. Nikolitsa Yannopoulou, yin@arg.op4.eu \*

Diploma Eng-EE, MEng-Telecom-EECE, PhD-Eng-Antennas-EECE  
Independent Researcher, Scheiblingkirchen, Austria  
Dr. Petros Zimourtopoulos, pez@arg.op4.eu \*

BSc-Physics, MSc-Radio-Electronics, PhD-Antennas-EE  
Independent Researcher, Scheiblingkirchen, Austria

\* Copy & Layout Editing - Proof Reading - Issue & Web Management

**Technical Support**

Konstantinos Kondylis, kkondylis@gmail.com

Diploma Eng-EECE, MEng-EECE, Doha, Qatar

Christos Koutsos, ckoutsos@gmail.com

Diploma Eng-EECE, MEng-EECE, Bratislava, Slovakia

**Information for Authors**

This is a small, but independent, low profile Journal, in which we are all—Authors, Reviewers, Readers, and Editors—free at last to be Peers in Knowledge, without suffering from Journal roles or positions, Professional–Amateur–Academic statuses, or established "impact factorizations", under the following guiding principles:

**Authors** – We know what Work means, we respect the Work of the Independent Researcher in Science and Engineering and we want to exhibit his Work. Thus, we decided to found this Free and Open Access Journal in which to publish this Work. Furthermore, as we care indeed for the Work of the technical author—especially a young or a beginner one—we strongly support the publication of his Work, as follows:

- 0 We do not demand from the author to transfer his own copyright to us. Instead, we only consider papers resulting from original research work only, and only if the author can assure us that he owns the copyright of his own paper as well as that he submits to the Journal either an original copy or a revised version of his own paper, for possible publication after review—or even for immediate republication, if this paper has already been published after review—but, in any case under a Creative Commons Attribution, CC-BY 3 Unported or CC-BY 4 International, License, only.
- 1 We encourage the author to submit his own paper written just in Basic English plus Technical Terminology.
- 2 We encourage the author even to select a pen name, which may drop it at any time to reveal his identity.
- 3 We encourage the author to submit an accepted for publication paper, which he was forced to decline that publication because it would be based on a review with unacceptable evaluation or derogatory comments.
- 4 We encourage the author to submit any paper that was rejected after a poor, impotent, inadequate, unreasonable, irresponsible, incompetent, or "just ticking" review.
- 5 We encourage the author to submit an unreviewed paper of his own that he uploaded on some Open Access repository.
- 6 We encourage the author to upload his published papers in our Journal to a truly Free Open repository like viXra.org.
- 7 We provide the author with a decent, express, peer review process, of up to just 4 weeks, by at least 2, either anonymous or onymous, reviewers.

8 We provide the author with the option to choose from 2 review processes: the traditional, anonymous, close one, as well as, a contemporary, onymous, open review in our private mailing list for Peer Discussion.

9 Under the Clause 0 : We immediately accept for publication a research paper directly resulting from a Project Report, or a Diploma-, Master-, or PhD-thesis, which already the author has successfully defended before a committee of experts, as long as he can mention 2 members of this committee who approved his Work.

10 Under the Clause 0 : We immediately accept for publication any paper which is not Openly Accessible on the Internet.

11 We immediately publish online a paper, as soon as it is accepted for publication in the Journal.

12 We quickly publish an extra issue—that is in excess of the 3 issues we publish a year—as soon as the review process of 3 papers is completed.

**Reviewers** – Every peer may voluntarily become a reviewer of the Journal in his skillfulness for as long as he wishes. In addition, each author of the Journal must review one paper in his expertness for each one of his published papers.

**Readers** – Every reader is a potential post-reviewer: we welcome comments and post-reviews in our private mailing list for Peer Discussion.

**Editors** – Every editor owns a PhD degree—to objectively prove that he really has the working experience of passing through the dominant publishing system. An editor pre-reviews a paper in order to check its compliance to our guiding principles and to select the appropriate reviewers of it. We can accept for consideration papers only in the expertise areas currently shown in the Editorial Team page, above. However, since we are very willing to amplify and extend the Scope of the Journal, we welcome the volunteer expert, in any related subject, who wants to join the Editorial Team as long as he unreservedly accepts our guiding principles.

### Electronic Publishing

We regularly use the Free Libre Open Source Software Libre Office with the Free Liberation Mono font and the Freewares PDFCreator and PDF-Xchange Viewer. We also use, with some basic html code of ours: the Free Open Source Software Open Journal System OJS by the Public Knowledge Project PKP installed in our website, and the Free Open Digital Library of

Internet Archive website, where we upload Issues, Paper reprints, *About* documents, and Volumes, in both portrait and landscape orientations, for exceptionally clear online reading with the Free Open Source BookReader.

### Submissions

We can consider only papers submitted in a format which is fully compatible with LibreOffice—preferably in odt format.

**Legal Notice** – It is taken for granted that the submitter—correspondent author accepts, without any reservation, the totality of our publication conditions as they are analytically detailed here, in this *About*, as well as, that he also carries, in the case of a paper by multiple authors, the independent will of each one of his coauthors to unreservedly accept all the aforementioned conditions for their paper.

### Internet Addresses

**Internet Publishing Website** : ftpj.otoiser.org

**Internet Archive Digital Library** : archive.org/details/@ftpj

**Printing-on-Demand** : pod@ftpj.otoiser.org

**Principal Contact** : principal-contact@ftpj.otoiser.org

**Technical Support** : technical-support@ftpj.otoiser.org

**Editorial Team–Technical Support List** : etts.ftpj.otoiser.org

**Peer Discussion List** : peers.ftpj.otoiser.org

**Submissions** : sub@ftpj.otoiser.org

**Sample Paper Template** : template.ftpj.otoiser.org

### ARG NfP AoI

Antennas Research Group

Not-for-Profit Association of Individuals \*

arg.op4.eu – arg@op4.eu

Hauptstraße 52, 2831 Scheiblingkirchen, Austria

\* The Constitution of Greece, Article: 12(3) 2008:

[www.hellenicparliament.gr/en/Vouli-ton-Ellinon/To-Politevma](http://www.hellenicparliament.gr/en/Vouli-ton-Ellinon/To-Politevma)

\* The Hellenic Supreme Court of Civil and Penal Law:

[www.areiospagos.gr/en/](http://www.areiospagos.gr/en/) – Court Rulings:Civil|A1|511|2008

---

*This document is licensed under a Creative Commons Attribution 4.0 International License – <https://creativecommons.org/licenses/by/4.0/>*

# Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 3: Short One-Port Calibration – Comparison

N. I. Yannopoulou, P. E. Zimourtopoulos \*

Antennas Research Group, Austria – Hellas [1, 2]  
EECE Dept, Democritus University of Thrace, Hellas [2]

## Abstract

In order to demonstrate the usefulness of the only one existing method for systematic error estimation in VNA (Vector Network Analyzer) measurements by using complex DERs (Differential Error Regions), we compare one-port VNA measurements after the two well-known calibration techniques: the quick reflection response, that uses only a single S (Short circuit) standard, and the time-consuming full one-port, that uses a triple of SLO standards (Short circuit, matching Load, Open circuit). For both calibration techniques, the comparison concerns: (a) a 3D geometric representation of the difference between VNA readings and measurements, and (b) a number of presentation figures for the DERs and their polar DEIs (Differential Error Intervals) of the reflection coefficient, as well as, the DERs and their rectangular DEIs of the corresponding input impedance. In this paper, we present the application of this method to an AUT (Antenna Under Test) selected to highlight the existence of practical cases in which the time consuming calibration technique results a systematic error estimation stripe including almost all of that of quick calibration.

## Introduction

The systematic error in a full one-port calibrated VNA measurement  $\rho$  of a given one-port DUT (Device Under Test) is already estimated by its DER [1]-[2]:

$$\rho = (m - D) / [M(m - D) + R] \quad (1)$$

$$d\rho = [-RdD - (m - D)^2dM - (m - D)dR + RdM] / [M(m - D) + R]^2 \quad (2)$$

where  $m$  is the VNA complex reading and  $D$ ,  $M$  and  $R$  are the complex system errors of Fig. 1.

The relations holding between this complex reflection

coefficient  $\rho$  and its respective impedance  $Z$ , as well as, between their DERs are [1]-[2]:

$$Z = Z_0(1 + \rho) / (1 - \rho) \quad (3)$$

$$dZ = 2Z_0d\rho / (1 - \rho)^2 \quad (4)$$

In this paper, we express the DERs for systematic error estimation in VNA measurements calibrated by the much simpler and quicker reflection response technique, in order to be in place to make some practical decisions from the different calibration techniques comparison.

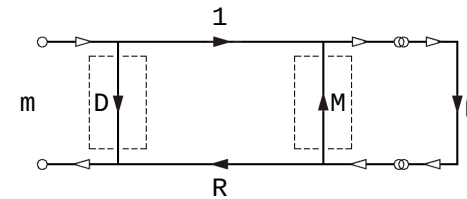


Fig. 1: Full one-port error model

## Response Calibration

The reflection response calibration technique can be accomplished with the measurement of only one standard load, instead of three in full one-port, usually of a S short circuit [3]-[4]. This means that the flow graph of Fig. 1 is simplified a lot, since the two surrounded by dashed boxes system error branches of directivity  $D$  and source match  $M$  do not exist, equivalently  $D = 0$  and  $M = 0$  and (1) results to:

$$R = m/\rho_S = s/S \quad (5)$$

where  $s$  is the VNA complex reading of the S short circuit standard with a nominal value of  $S = -1$ ,  $m$  is the complex reading of a given DUT and  $\rho_S$  is its complex reflection coefficient as it is measured after this response calibration:

$$\rho_S = (m/s)S \quad (6)$$

which, from (2), has the differential error:

$$d\rho_S = (S/s)dm - (Sm/s^2)ds + (m/s)dS \quad (7)$$

The corresponding total DER is then the sum of  $L = 3$  parallelograms. Therefore, this DER contour is a polygonal line with  $4L = 12$  line segments and vertices at most, in contrast with the DER of the measurement after a SLO full one-port calibration, which is a piecewise curve composed of  $4(L - 1) = 24$  line segments,  $4(L - 1) = 24$  circular arcs and  $8(L - 1) = 48$  vertices, at most [1]-[2].

## Application Results

By following the error estimation process, we already detailed in [1]-[2], we take as  $dS$  the considered manufacturers' standard S uncertainty data:

$$-0.01 \leq d|S| \leq 0, \quad -2^\circ \leq d\angle S \leq +2^\circ$$

and as  $dm$  and  $ds$  the VNA inaccuracy of  $\pm 1$  digit in LSD of their corresponding readings, for either the amplitude in decibels or the phase in degrees. Moreover, the one-port DUT that was considered is the same typical UHF ground-plane antenna (that is: AUT) mentioned in [1].

The difference between the 3 nominal values (-1, 0, 1) of the 3 full one-port calibration standards (S, L, 0), respectively, and their 3 corresponding VNA readings ( $s$ ,  $l$ ,  $o$ ), can be estimated by the extent of the surfaces shown in the triptych of Fig. 2, where the vertical axis segment represents the range of the distinct stepped frequencies. Each surface is formed by parallel to horizontal plane lines. Each such line expresses the complex difference between the standard nominal value and its corresponding VNA reading, in each stepped frequency.

In the triptych of Fig. 3, and from left to right we have the difference surfaces made by distance lines between:

(a) the measured reflection coefficient  $\rho$  after a full SLO one-port calibration (black solid points) and the corresponding VNA readings  $m$  for the AUT measurement (colored magenta points),

(b) the measured reflection coefficient  $\rho_s$  after S response calibration (black ring points) and the corresponding VNA readings  $m$  for the AUT measurement (colored magenta points), and

(c) the two measurements ( $\rho$ ,  $\rho_s$ ).

All the involved, previously shown, quantities are projected on the horizontal complex plane of Fig. 4. The magenta colored spiral represents  $m$ , while, the black curves the reflection coefficient: solid points, for  $\rho$ , and ring points for  $\rho_s$ . All of 1 VNA readings are close enough to complex origin (colored green points). It is rather difficult to distinguish the two curves for  $s$  and  $o$  VNA readings, which are close enough to the unit circle circumference (colored red solid points and colored blue ring point, respectively).

The  $\rho$ -DERs and  $\rho_s$ -DERs, for all 4 MHz stepped frequencies covering the range of [600, 1000] MHz, are overlapped on the complex plane of Fig. 5, forming a light and a dark gray stripes, respectively. From each stripe we selected 11 DERs out of 101, drawn with dark gray and white colors respectively, to illustrate their outline dependence on frequency.

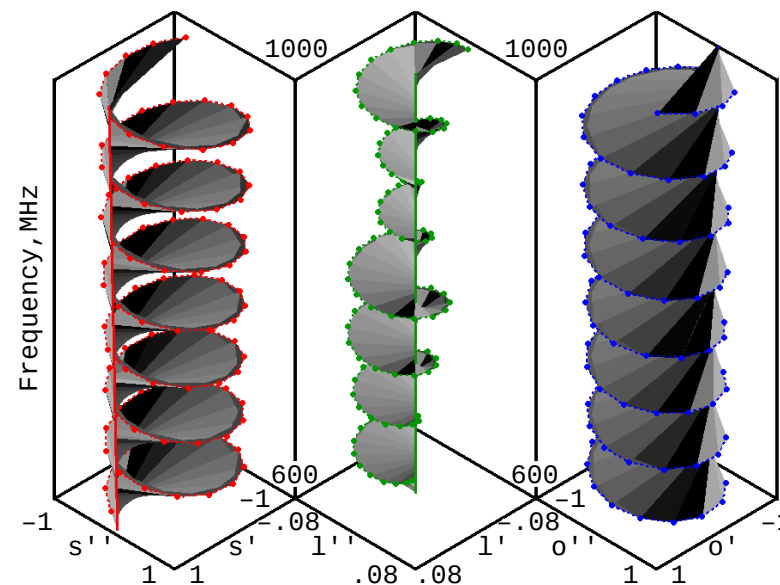


Fig. 2: Difference between  $s$  and  $S$ ,  $l$  and  $L$ ,  $o$  and  $O$

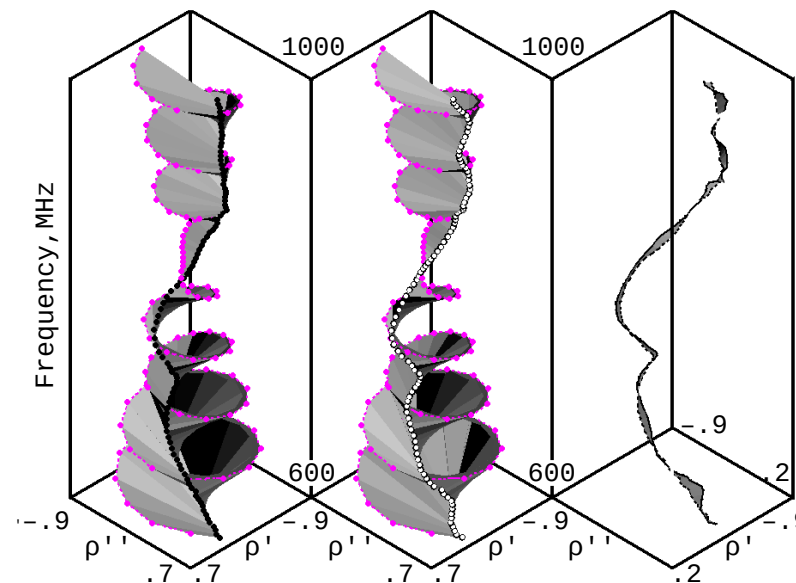


Fig. 3: Difference between  $m$  and  $\rho$ ,  $m$  and  $\rho_s$ ,  $\rho$  and  $\rho_s$ .



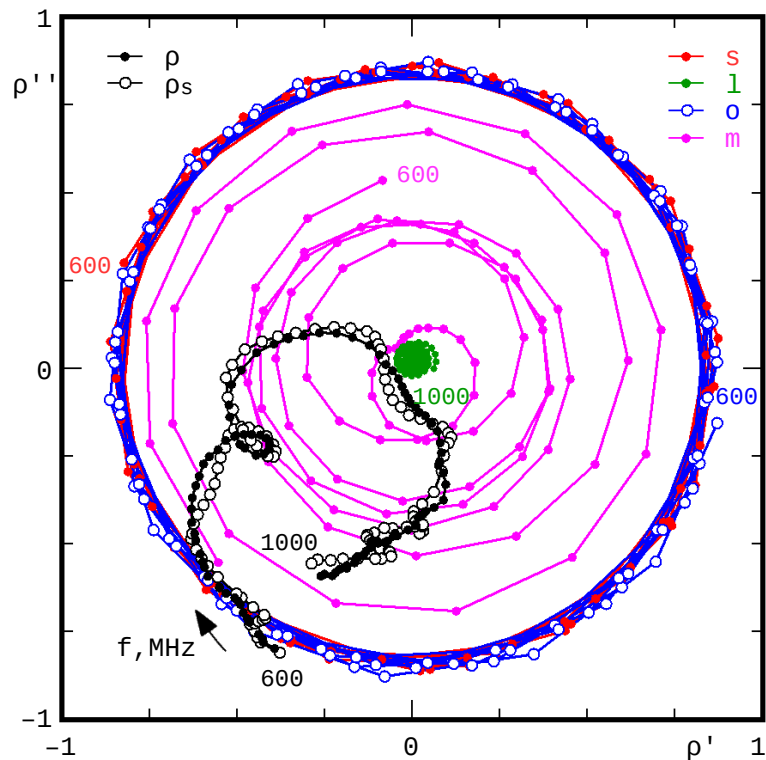


Fig. 4: VNA s, l, o, m readings and  $\rho$ ,  $\rho_s$  measurements.

Moreover, we selected to magnify a part of this figure in the sub-range of [892, 1000] MHz, to further illustrate the DER outlines and their overlapping in Fig. 6, where the clearly shown ripple of the simple response calibration stripe over the relatively smooth full one-port calibration stripe reveals the superiority of the latter in the production of more accurate measurements.

The comparison between the AUT measurements based on

these two calibration techniques is extended to the comparison against the frequency:

(a) of the computed polar DEIs of the reflection coefficient magnitude and argument stripes in Fig. 7,

(b) of the rectangular DEIs for the corresponding R input resistance and X input reactance stripes, in Fig. 8 and

(c) of the Z-DERs, and  $Z_s$ -DERs stripes in Fig. 9.

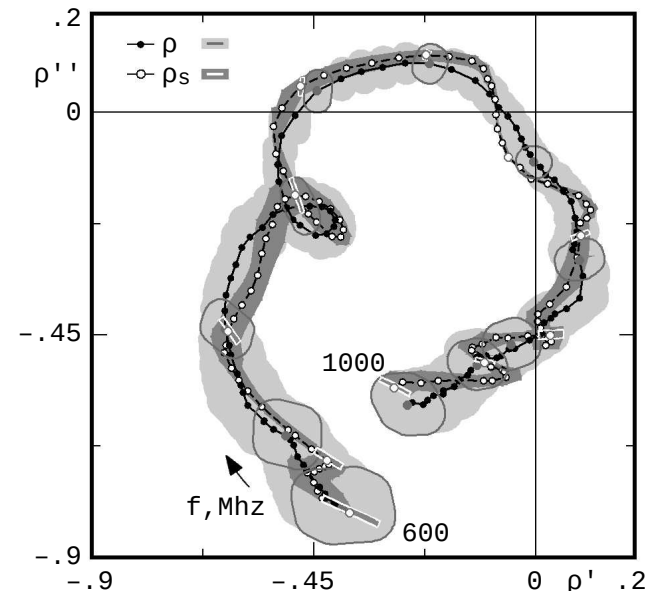


Fig. 5: Complex  $\rho$ -DERs and  $\rho_s$ -DERs in [600, 1000] MHz

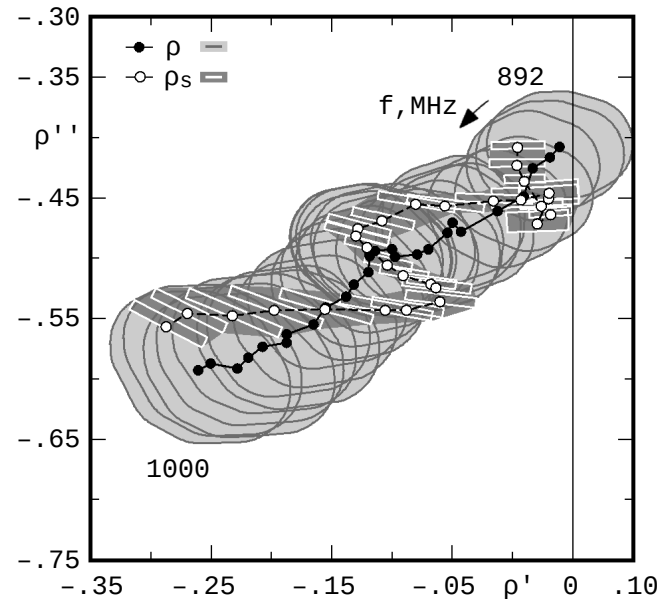


Fig. 6: Complex  $\rho$ -DERs and  $\rho_s$ -DERs in [892, 1000] MHz

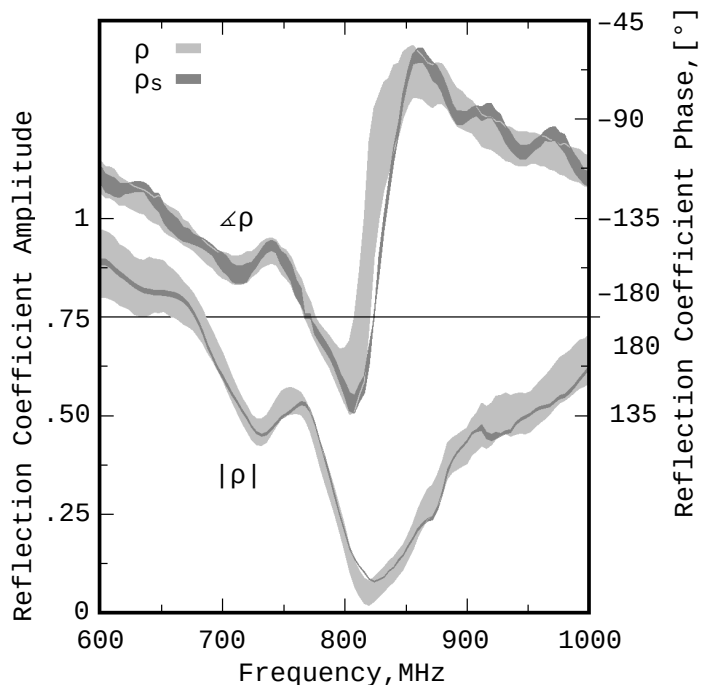


Fig. 7: Polar DEIs of reflection coefficient

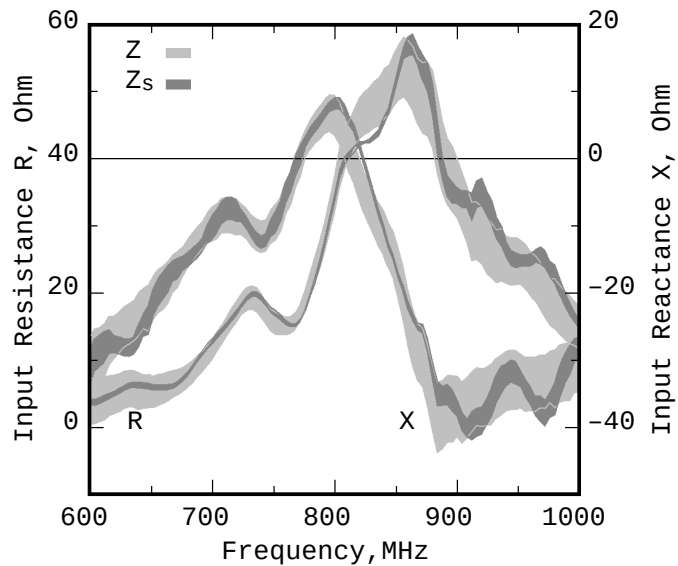


Fig. 8: Rectangular DEIs of input impedance

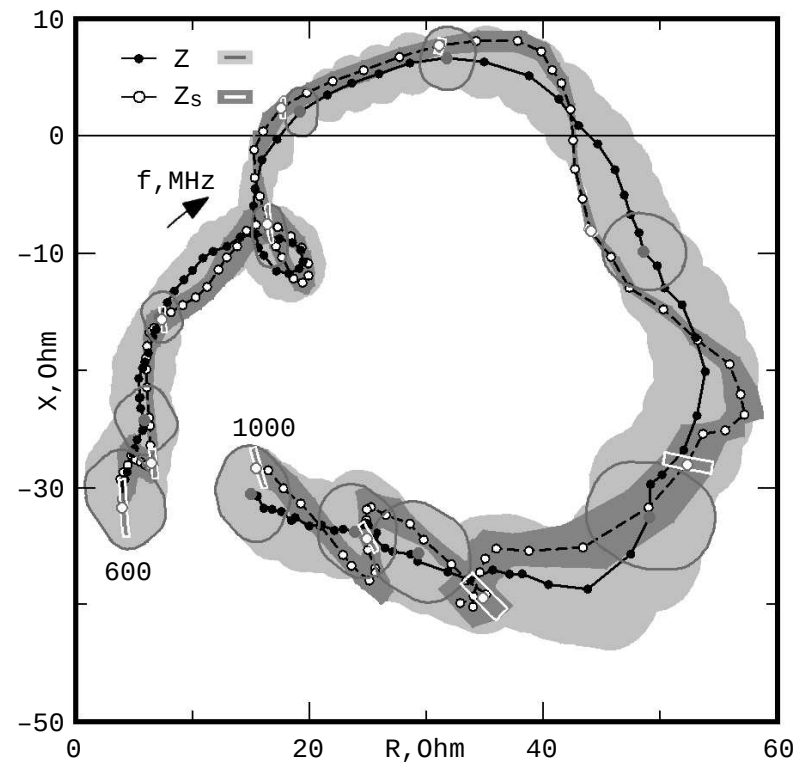


Fig. 9: Complex Z-DERs and  $Z_s$ -DERs in [600, 1000] MHz

**Conclusion**

From all that, it must be clear now that in this intentionally selected for presentation particular AUT case there was no advantage at all

in selection of full one-port calibration over the reflection response one, due to their remarkable in all aspects coincidence. Of course this is just another one conclusion a-posteriori.

**References \***

[ This Page Intentionally Left Blank ]

- [1] Yannopoulou N., Zimourtopoulos P., "Total Differential Errors in One Port Network Analyzer Measurements with Application to Antenna Impedance", Radioengineering, Vol. 16, No. 2, June 2007, pp. 1-8  
"www.radioeng.cz/fulltexts/2007/07\_02\_01\_08.pdf"
  - [2] Yannopoulou N.I., Zimourtopoulos P.E., "Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 1: Full One-Port Calibration", FunkTechnikPlus # Journal, Issue 1, October 2013, pp. 17-22  
"www.otoiser.org/index.php/ftpj/article/view/42"
  - [3] HP, "Vector Measurements of High Frequency Networks", Hewlett-Packard, 1989, pp. 2-13, 2-15, 3-11, 3-12
  - [4] AGILENT, "OPEN/SHORT Response Calibration (reflection test), Calibration Types and Characteristics"  
"http://ena.support.keysight.com/e5071c/manuals/webhelp/eng/measurement/calibration/calibration.htm"
- \*Active Links: 15.12.2013 - Inactive Links : FTP#J Link Updates: "http://updates.ftpj.otoiser.org/"

**Preprint Versions**

"Comparison of Error Estimation by DERs in One-Port S and SLO Calibrated VNA Measurements and Application"  
Nikolitsa Yannopoulou, Petros Zimourtopoulos  
"http://arxiv.org/abs/1102.4239"

**Follow-Up Research Paper**

Not until now

**Previous Publication in FUNKTECHNIKPLUS # JOURNAL**

"Measurement Uncertainty in Network Analyzers: Differential Error Analysis of Error Models Part 2: Full Two-Port Calibration", Issue 1, pp. 23-30

**\* About The Authors**

*Nikolitsa Yannopoulou*, Issue 1, p. 15

*Petros Zimourtopoulos*, Issue 1, p. 15

---

*This paper is licensed under a Creative Commons Attribution 4.0 International License – <https://creativecommons.org/licenses/by/4.0/>*



[ This Page Intentionally Left Blank ]

[ This Page Intentionally Left Blank ]

[ This Page Intentionally Left Blank ]

In case of any doubt,  
download the genuine papers from  
[genuine.ftpj.otoiser.org](http://genuine.ftpj.otoiser.org)

#### FRONT COVER VIGNETTE

A faded synthesis of an anthemion rooted in a meandros

The thirteen-leaf is a symbol for a life tree leaf.  
"Herakles and Kerberos", ca. 530–500 BC,  
by Paseas, the Kerberos Painter,  
Museum of Fine Arts, Boston.

[www.mfa.org/collections/object/plate-153852](http://www.mfa.org/collections/object/plate-153852)

The simple meandros is a symbol for eternal immortality.  
"Warrior with a phiale", ca. 480–460 BC,  
by Berliner Maler,  
Museo Archeologico Regionale "Antonio Salinas" di Palermo.

[commons.wikimedia.org/wiki/File:Warrior\\_MAR\\_Palermo\\_NI2134.jpg](https://commons.wikimedia.org/wiki/File:Warrior_MAR_Palermo_NI2134.jpg)